Last time Graussian Eliun Solution Paradigms A linear system has 3 possible soltin paradigms: -> No solutions * (from an inconsistent equation) -> Exactly 1 Sol. Lm * -> Infinitely many solutions < X This These are the only three possibilities ... Goal: Determine Solution Sets. In general we give a full set of Column vectors Ex: Last the ne solved $\begin{cases} 2 \times & +2 + h = 5 \\ 3 \times & -2 - v = 0 \\ 4 \times & +y + 22 + w = 9 \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 \times & 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 \times & 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 \times & 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 \times & 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 \times & 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 \times & 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 \times & 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 \times & 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 \times & 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y =$ we write the solution set like so: $\begin{bmatrix} -1 & +t \\ 5 & -t \end{bmatrix} = \begin{bmatrix} 0 \\ -1 \\ 5 \end{bmatrix} + \begin{bmatrix} 0 \\ -t \\ t \end{bmatrix} = \begin{bmatrix} 0 \\ -1 \\ 5 \end{bmatrix} + t \begin{bmatrix} 0 \\ -1 \\ 5 \end{bmatrix} + t \begin{bmatrix} 0 \\ -1 \\ 5 \end{bmatrix} + t \begin{bmatrix} 0 \\ -1 \\ 5 \end{bmatrix} + t \begin{bmatrix} 0 \\ -1 \\ 5 \end{bmatrix}$ MB: this vector is a particular solution ...

Matrices

A matrix is a rectangular array of numbers

[3 2]
[0 0 5]
[1.1]

2x2

An man matrix has m rows an u columns

A column vector is an NXI matrix.

A von vector is a 1xn matrix.

The entries of a matrix are the numbers in the notion Entries are indexed by row and column.

Ex: $A = \begin{bmatrix} 0 & 1 & -1 & 2 & 5 \\ 1 & 0 & -3 & 0 & 2 \\ 0 & 0 & 0 & 7 \end{bmatrix}$ Column

Number

Number

Convention: Matrices are represented of Capital letters.

the corresponding entries are repid by the lowerex letter, so $D = \int d_{i,j}$.

We can represent a linear system via an arguented matrix.

 $Ex: \begin{cases} 3x + 59 - 72 + w = 0 \\ 59 - 32 + v = 5 \\ x - 2 = 6 \end{cases} \begin{bmatrix} 3 & 5 - 7 & 1 & 0 \\ 0 & 5 & -3 & 1 & 5 \\ 1 & 0 & -1 & 0 & 6 \end{bmatrix}$

Let's solve this system u/ its matrix representation

translates into "ron operations" NB: Gaussian elimination for the natrix setup. Sol: [3 5 -7 1 0] (3 col. [1 0 -1 0 6] 5 [3 col. [3 5 -3 1 5] 5 [3 col. [3 5 -7 1 0] 6] [3 col. [3 5 -7 1 0] $\frac{\beta_{3}-3\beta_{1}}{0} \begin{bmatrix} 1 & 0 & -1 & 0 & | & 6 \\ 0 & 5 & -3 & 1 & | & 5 \\ 0 & 5 & -4 & 1 & | & -18 \end{bmatrix} \xrightarrow{\beta_{3}-\beta_{2}} \begin{bmatrix} 1 & 0 & -1 & 0 & | & 6 \\ 0 & 5 & -3 & 1 & | & 5 \\ 0 & 0 & -1 & 0 & | & -23 \end{bmatrix}$ (lence he has solthon set $\begin{cases} 29 \\ 74 \\ 5 \\ 23 \end{cases}$; $t \in \mathbb{R}$) OR $\{\begin{bmatrix} 29 \\ 0 \\ 23 \end{bmatrix} + S \begin{bmatrix} 0 \\ 0 \\ -5 \end{bmatrix} : SER \}$ Some solution set, [A]

Ex: Solve
$$\begin{cases} x_1 & +x_3 = 4 \\ x_1 & -x_2 + 2x_3 = 5 \\ 4x_1 & -x_2 + 5x_3 = 17 \end{cases}$$

$$\begin{cases} x_1 & 1 \times_3 = 4 \\ x_2 & - \times_3 = -1 \end{cases} \sim_{x_1} \begin{cases} x_1 = 4 - t \\ x_2 = -1 + t \\ x_3 = t \end{cases}$$

: Solution set is
$$\left\{\begin{bmatrix}4\\1\\0\end{bmatrix}+t\begin{bmatrix}1\\1\end{bmatrix}:t\in\mathbb{R}\right\}$$

Preview of Coming Attactions: Matrix Algebra. Operations on natrices (today): -> Normal row operations (sup, all, notifly). maker in this interior Defn: Let A and B be non matrices
and let c ER be constant.

The Sum of A and B is $A+B = \begin{bmatrix} a_{i1} + b_{ij} \end{bmatrix}$, i.e. the under obtained by entry-wise addition.

The Scalar unlittle of A by (is $A = \begin{bmatrix} ca_{ij} \end{bmatrix}$), i.e. the matrix obtained from an Hiphyny each entry of A by (is $A = \begin{bmatrix} ca_{ij} \end{bmatrix}$).

Ex: $\begin{bmatrix} 3 & -1 & 0 \\ 2 & 0 & 1 \end{bmatrix} + \begin{bmatrix} 7 & -1 & 0 \\ 0 & -1 & -1 \end{bmatrix} = \begin{bmatrix} 3+1 & -1-1 & 0+0 \\ 2+0 & 0-1 & 1-1 \end{bmatrix} = \begin{bmatrix} 10 & -2 & 0 \\ 2+0 & 0-1 & 1-1 \end{bmatrix}$ S $\begin{bmatrix} 2 & 3 \\ 1 & 3 \end{bmatrix} = \begin{bmatrix} 5 & 2 & 5 & 3 \\ 5 & 1 & 5 & -3 \end{bmatrix} = \begin{bmatrix} 10 & 15 \\ 5 & -15 \end{bmatrix}$ Non-ex: $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 5 \end{bmatrix} + \begin{bmatrix} 3 & 0 \\ 0 & 3 & 7 & -2 \end{bmatrix}$ TS UNDEFINED!